

5.6 Properties of Linear Relations

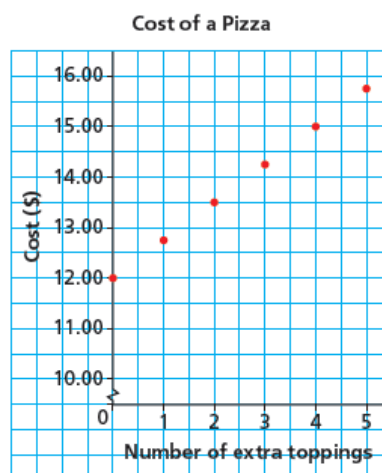
LESSON FOCUS

Identify and represent linear relations in different ways.

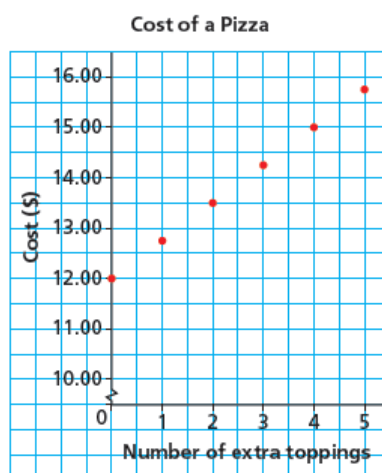
Make Connections

The table of values and graph show the cost of a pizza with up to 5 extra toppings.

Number of Extra Toppings	Cost (\$)
0	12.00
1	12.75
2	13.50
3	14.25
4	15.00
5	15.75



Number of Extra Toppings	Cost (\$)
0	12.00
1	12.75
2	13.50
3	14.25
4	15.00
5	15.75



What patterns do you see in the table?

Write a rule for the pattern that relates the cost of a pizza to the number of its toppings.

How are the patterns in the table shown in the graph?

How can you tell from the table that the graph represents a linear relation?

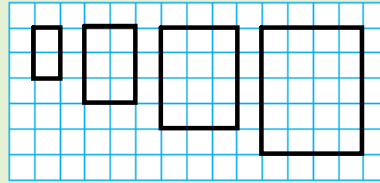
TRY THIS

Work with a partner.

You will need 1-cm grid paper.

Use this pattern of rectangles.

This pattern continues.



A. Draw the next two rectangles in the pattern.

Copy and complete each table of values for the 6 rectangles.

Width of Rectangle (cm)	Area (cm^2)
1	
2	

Width of Rectangle (cm)	Perimeter (cm)
1	
2	

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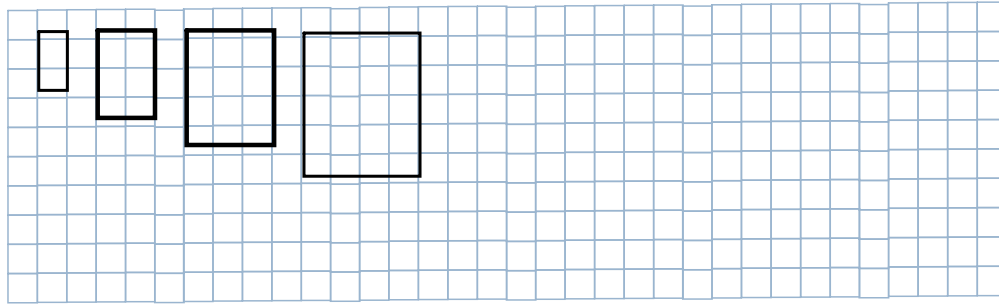
TRY THIS (continued)

B. Which table of values represents a linear relation? How can you tell?

C. Graph the data in each table of values.
Does each graph represent a linear relation?
How do you know?

5.6 Properties of Linear Relations

Draw the next two rectangles in the pattern.



Copy and complete each table of values for the 6 rectangles.

Width of Rectangle (cm)	Area (cm ²)

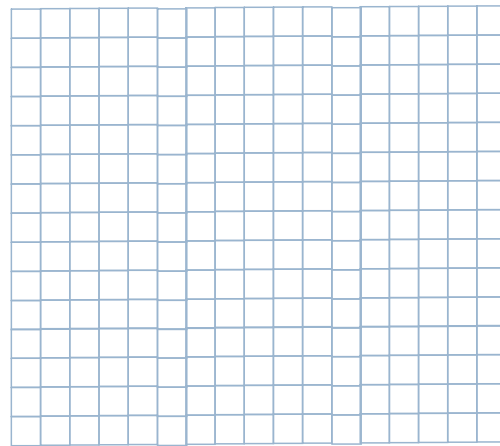
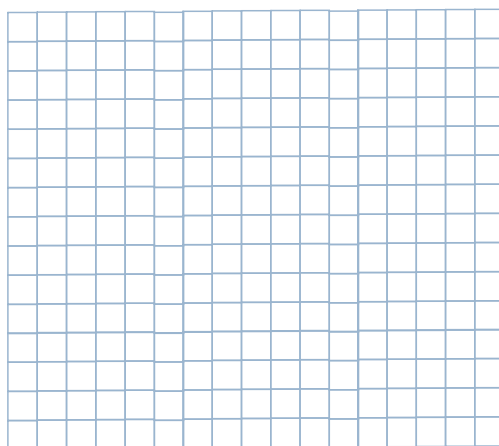
Width of Rectangle (cm)	Perimeter (cm)

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Which table of values represents a linear relation? How can you tell?

Graph the data in each table of values.

Does each graph represent a linear relation? How do you know?



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* The cost for a car rental is \$60, plus \$20 for every 100 km driven.
The independent variable is the ? and the dependent variable is ?

→ We can identify that this is a linear relation in different ways. *

#1 a table of values

Distance (km)	Cost (\$)
0	60
100	80
200	100
300	120
400	140

* ?

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Tuesday, November 29th

- Review notes from section 5.6
- Look over a few examples (copy into notes)
- Classwork/Homework

Please note: Extra help will now be offered
on Mondays and Thursdays (11:50 - 12:20)

We can identify that this is a linear relation in different ways. *

#1 a table of values

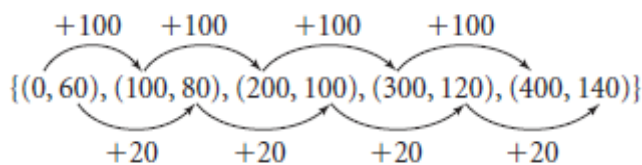
x # of Km	y Cost (\$)
0	60
+100	80
+100	100
+100	120
+100	140

\$60 to rent
a car
and
\$20/100 Km

#2 a set of ordered pairs

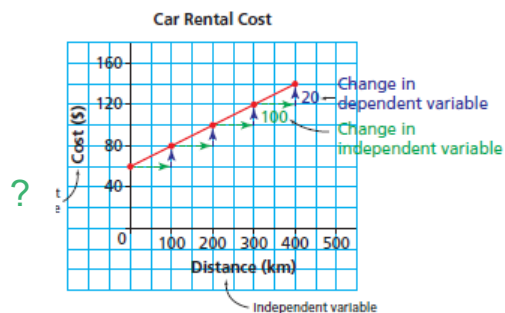
The difference in each x-value must be equal.

The difference in each y-value must also be equal.



#3 a graph

A linear relation's graph will be one straight line in any direction.



We can use each representation (aka "slope") to calculate the rate of change.

The rate of change can be expressed as a fraction:

$$\begin{aligned} & \frac{\text{change in dependent variable (y)}}{\text{change in independent variable (x)}} = \frac{\$20}{100 \text{ km}} \\ & = \$0.20/\text{km} \end{aligned}$$

The rate of change is \$0.20/km; that is, for each additional 1 km driven, the rental cost increases by 20¢. The rate of change is constant for a linear relation.

We can determine the rate of change from the equation that represents the linear function.

Let the cost be C dollars and the distance driven be d kilometres.

An equation for this linear function is:

$$C = 0.20d + 60$$

Dependent variable

?

?

?

?

Example 1**Determining whether a Table of Values Represents a Linear Relation**

Which table of values represents a linear relation? Justify the answer.

- a) The relation between temperature in degrees Celsius, C , and temperature in degrees Fahrenheit, F

	C	F
+5	0	32
+5	5	41
+5	10	50
+5	15	59
+5	20	68

- b) The relation between the current, I amps, and power, P watts, in an electrical circuit

	I	P
+5	0	0
+5	5	75
+5	10	300
+5	15	675
+5	20	1200

**SOLUTION**

rate of change:
 $\frac{9}{5} = 1.8$

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CHECK YOUR UNDERSTANDING

When an equation is written using the variables x and y , x represents the independent variable and y represents the dependent variable.

Example 2**Determining whether an Equation Represents a Linear Relation**

- a) Graph each equation.

i) $y = -3x + 25$

ii) $y = 2x^2 + 5$

iii) $y = 5$

iv) $x = 1$

- b) Which equations in part a represent linear relations?
 How do you know?

**SOLUTION**

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CHECK YOUR UNDERSTANDING

Example 2

Determining whether an Equation Represents a Linear Relation

a) Graph each equation.

i) $y = -3x + 25$

Creating a table of values

x	y
0	25
1	22
2	19
3	16
4	13

Changes in y: -3, -3, -3, -3

ii) $y = 2x^2 + 5$

x	y
-2	13
-1	7
0	5
1	7
2	13

Changes in y: -6, -2, +2, +6

iii) $y = 5$

iv) $x = 1$

b) Which equations in part a represent linear relations?
How do you know?

Example 3

Identifying a Linear Relation

Which relation is linear? Justify the answer.

a) A new car is purchased for \$24 000. Every year, the value of the car decreases by 15%. The value is related to time.

x (time)	y (cost) value
0	24 000
1	20 400
2	17 340
3	14 739
4	

Changes in y: -3600, -3060

85%
 $\frac{85}{100} = 0.85$

b) For a service call, an electrician charges a \$75 flat rate, plus \$50 for each hour he works. The total cost for service is related to time.

x (time)	y (cost)
0	75
1	125
2	175
3	225
4	275

Changes in y: +50, +50, +50, +50

SOLUTION

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Pg. 308-309

3-6

Wednesday, November 30th

- Warm-up #8
- Check and go over homework Pg.308 #3-6
- Review an example on finding rate of change
- Classwork/Homework

Please note: Extra help will now be offered on Mondays and Thursdays (11:50 - 12:20)

Warm-up #8

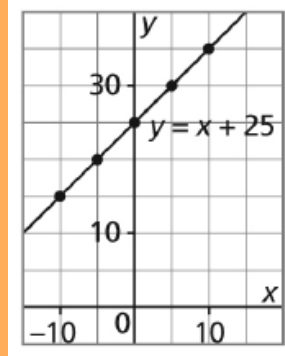
Nov. 30

#1 Are the following linear relations? Show or explain why.

a)

t	n
0	1
20	2
40	4
60	8
80	16
100	32

b)



#2 a. Create a table of values for each of the following.

b. Tell me whether each is a linear relation or not?

a)

$$y = x^2 + 25$$

b)

$$y = x + 25$$

Please open your notebook to the answers to the following questions:

Pg. 308-309 #3-6

3. Which tables of values represent linear relations? Explain your answers.

a)

Time (min)	Distance (m)
0	10
2	50
4	90
6	130

b)

Time (s)	Speed (m/s)
0	10
1	20
2	40
3	80

c)

Speed (m/s)	Time (s)
15	7.5
10	5
5	2.5
0	0

d)

Distance (m)	Speed (m/s)
4	2
16	4
1	1
9	3



3. a) Linear relation
c) Linear relation

b) Not a linear relation
d) Not a linear relation

4. Which sets of ordered pairs represent linear relations? Explain your answers.

a) $\{(3, 11), (5, 9), (7, 7), (9, 5)\}$

b) $\{(-2, 3), (0, 1), (2, -3), (4, -7)\}$

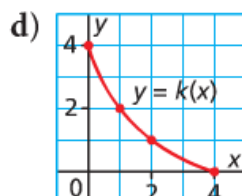
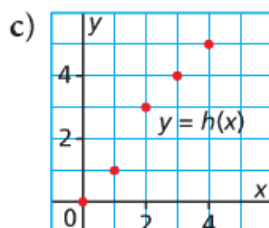
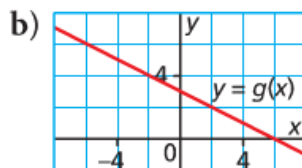
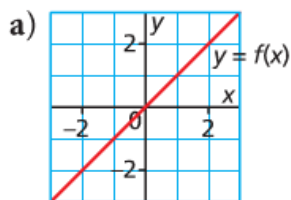
c) $\{(1, 1), (1, 3), (2, 1), (2, 3)\}$



4. a) Linear relation
c) Not a linear relation

b) Not a linear relation

5. Which graphs represent linear relations? How do you know?



5. a) Linear relation b) Linear relation
c) Not a linear relation d) Not a linear relation

6. a) Create a table of values when necessary, then graph each relation.

i) $y = 2x + 8$

ii) $y = 0.5x + 12$

iii) $y = x^2 + 8$

iv) $y = 2x$

v) $x = 7$

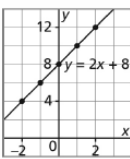
vi) $x + y = 6$

b) Which equations in part a represent linear relations? How do you know?

6. a) Tables of values may vary. For example:

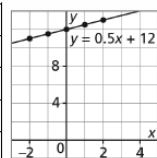
i)

x	y
-2	4
-1	6
0	8
1	10
2	12



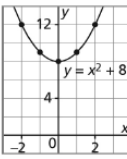
ii)

x	y
-2	11
-1	11.5
0	12
1	12.5
2	13



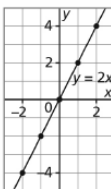
iii)

x	y
-2	12
-1	9
0	8
1	9
2	12



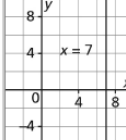
iv)

x	y
-2	-4
-1	-2
0	0
1	2
2	4



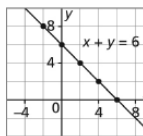
v)

x	y
-2	8
-1	7
0	6
1	5
2	4
3	3
4	2
5	1
6	0
7	-1
8	-2



vi)

x	y
-2	8
0	6
2	4
4	2
6	0



b) The relations in part a, i, ii, iv, v, and vi are straight lines, so they are linear relations.

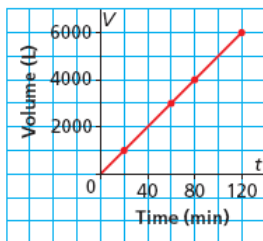
Example 4**Determining the Rate of Change of a Linear Relation from Its Graph**

A water tank on a farm near Swift Current, Saskatchewan, holds 6000 L.

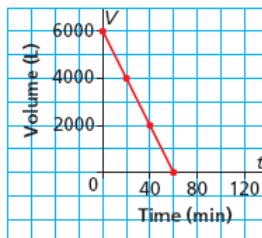
Graph A represents the tank being filled at a constant rate.

Graph B represents the tank being emptied at a constant rate.

Graph A
Filling a Water Tank



Graph B
Emptying a Water Tank



- Identify the independent and dependent variables.
- Determine the rate of change of each relation, then describe what it represents.

CHECK YOUR UNDERSTANDING

5.6 Properties of Linear Relations



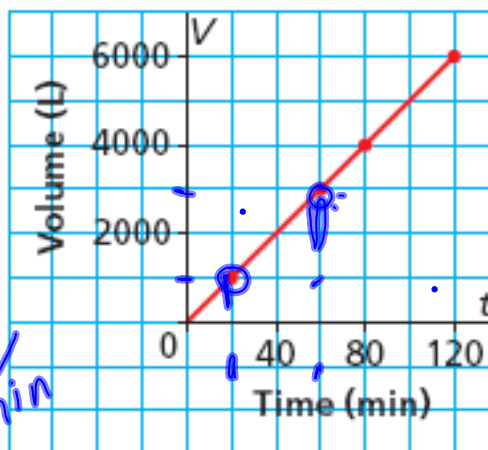
SOLUTION

Rate of change

$$\frac{\text{change of dep. (y)}}{\text{change of ind. (x)}}$$

$$\frac{2000}{40} = 50 \text{ L/min}$$

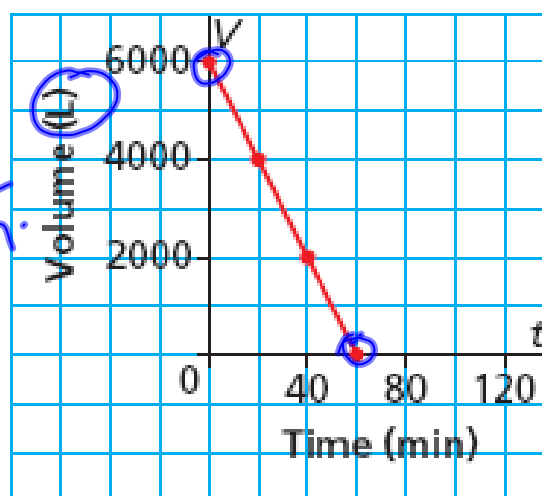
Graph A
Filling a Water Tank



$$\frac{\Delta y}{\Delta x}$$

$$\frac{6000}{60} = 100 \text{ L/min}$$

Graph B
Emptying a Water Tank



Classwork/Homework

Page 308-310 #7-10,12,14

